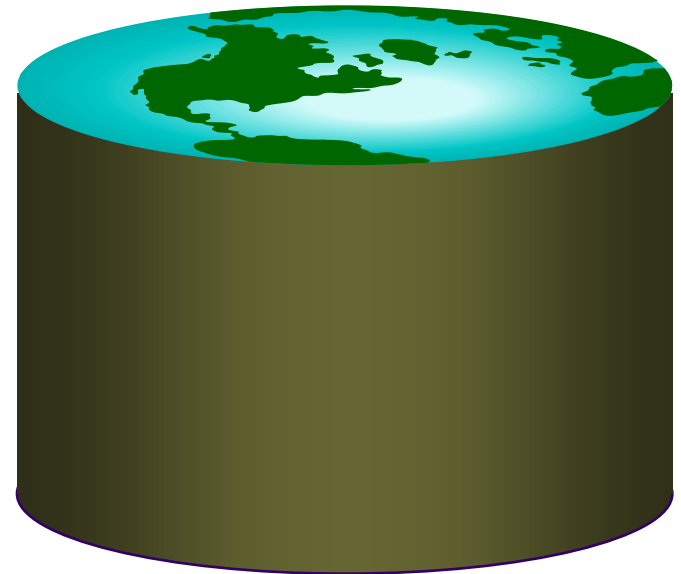


CS 405G: Introduction to Database Systems

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Review

- The unit of disk read and write is
 - Block (or called Page)
- The disk access time is composed by
 - Seek time
 - Rotation time
 - Data transfer time

Review

- A row in a table, when located on disks, is called
 - A record
- Two types of record:
 - Fixed-length
 - Variable-length

Review

- In an abstract sense, a file is
 - A set of “records” on a disk
- In reality, a file is
 - A set of disk pages
- Each record lives on
 - A page
- Physical Record ID (RID)
 - A tuple of $\langle \text{page\#}, \text{slot\#} \rangle$

Today's Topic

- How to locate data in a file *fast*?
- Introduction to indexing
- Tree-based indexes
 - ISAM: Indexed sequence access method
 - B⁺-tree

Basics

- Given a value, locate the record(s) with this value

SELECT * FROM R WHERE $A = value$;

SELECT * FROM R, S WHERE $R.A = S.B$;

- Other search criteria, e.g.

- Range search

SELECT * FROM R WHERE $A > value$;

- Keyword search

database indexing

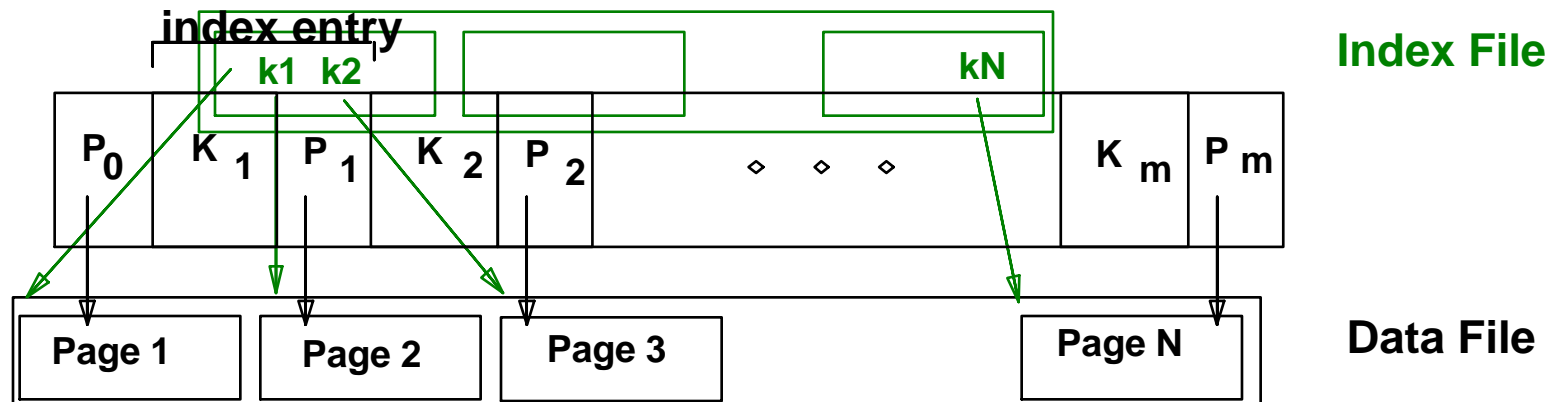
Search

Tree-Structured Indexes: Introduction

- Tree-structured indexing techniques support both *range selections* and *equality selections*.
- ISAM = Indexed Sequential Access Method
 - static structure; early index technology.
- B^+ tree: dynamic, adjusts gracefully under inserts and deletes.

Motivation for Index

- ``Find all students with $gpa > 3.0$ ``
 - If data file is sorted, do binary search
 - Cost of binary search in a database can be quite high, Why?
- Simple idea: Create an `index` file.

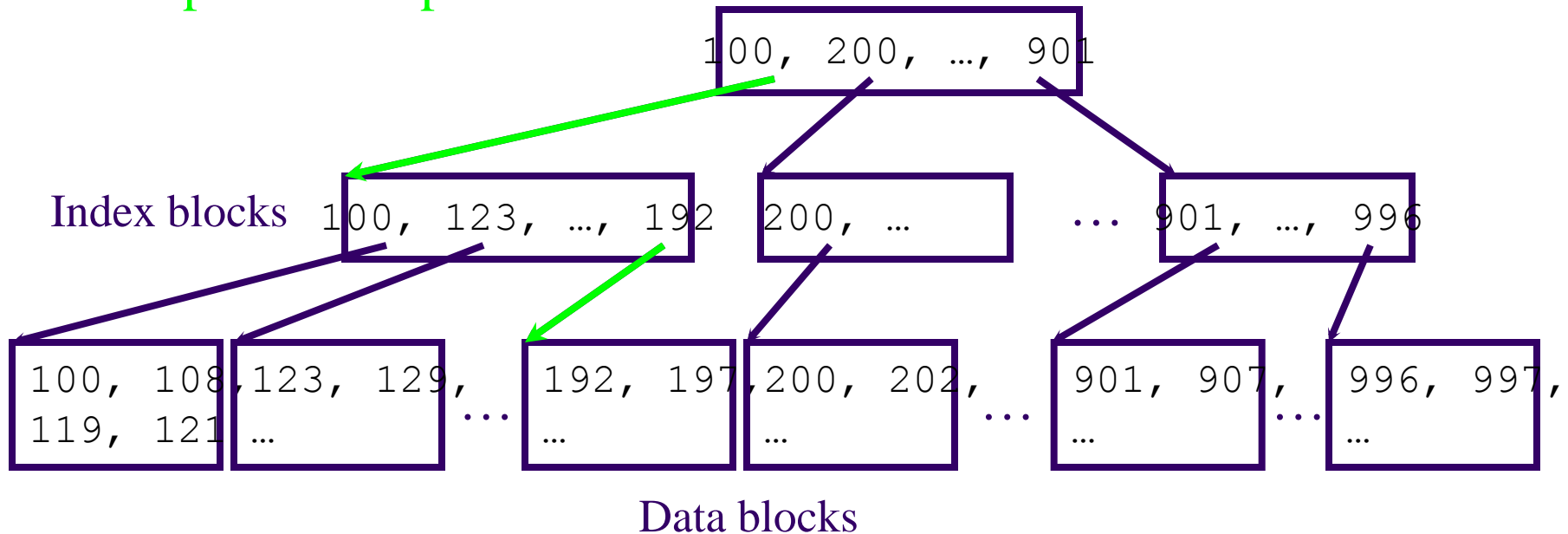


Can do binary search on (smaller) index file!

ISAM

- What if an index is still too big?
 - Put a another (sparse) index on top of that!
 - ☞ ISAM (Index Sequential Access Method), more or less

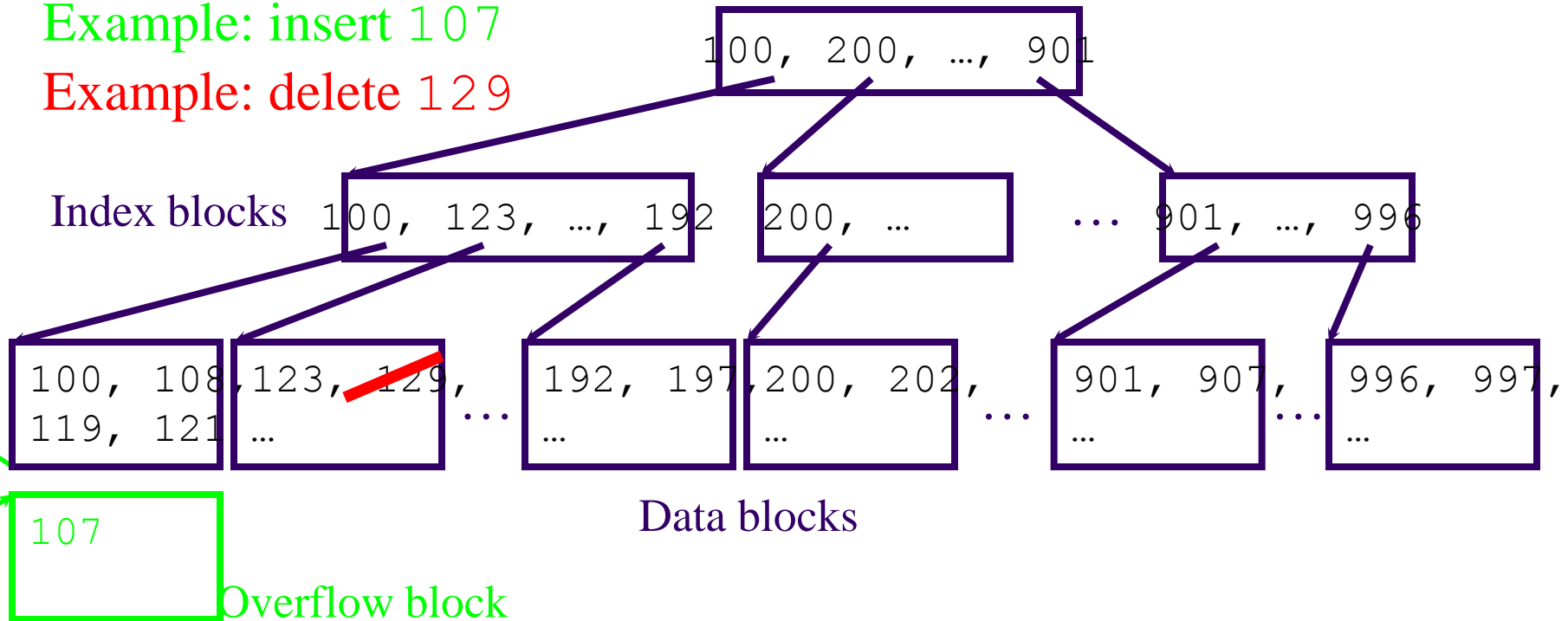
Example: look up 197



Updates with ISAM

Example: insert 107

Example: delete 129



- Overflow chains and empty data blocks degrade performance
 - Worst case: most records go into one long chain

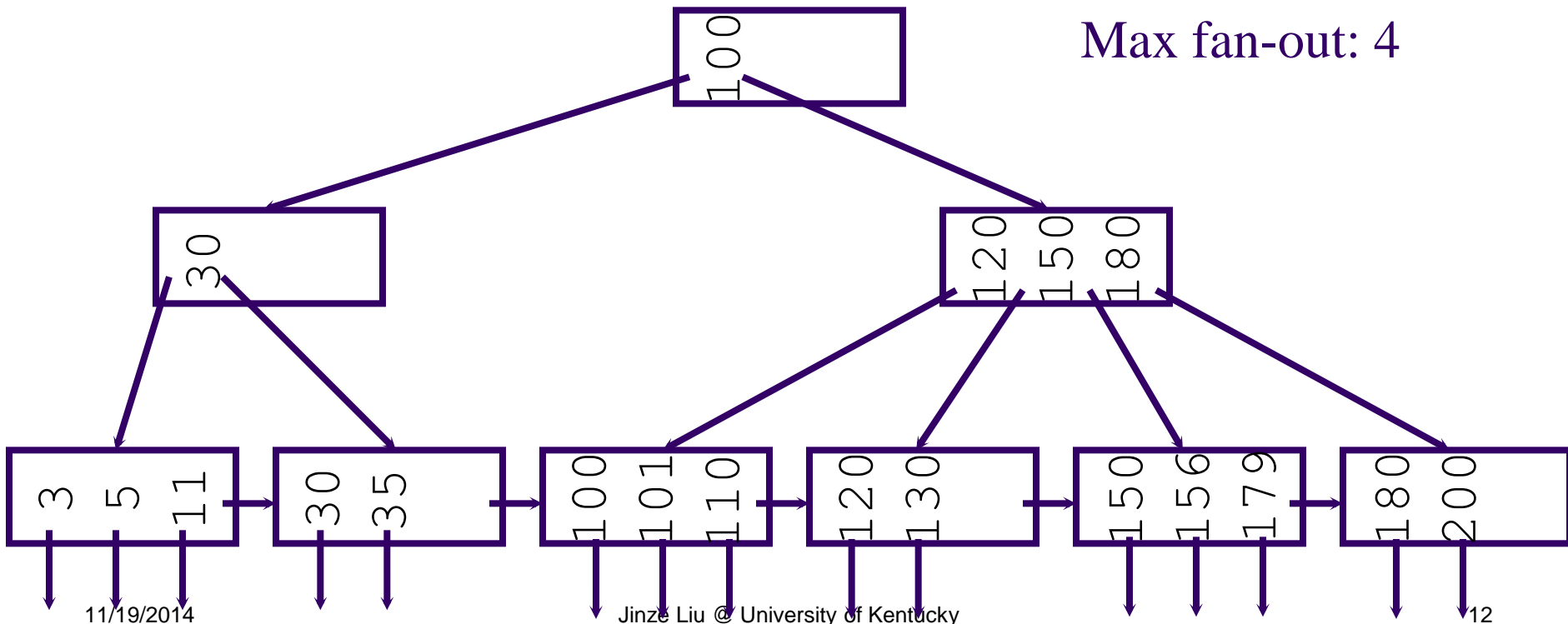
A Note of Caution

- ISAM is an old-fashioned idea
 - B⁺-trees are usually better, as we'll see
- But, ISAM is a good place to start to understand the idea of indexing
- Upshot
 - Don't brag about being an ISAM expert on your resume
 - Do understand how they work, and tradeoffs with B⁺-trees

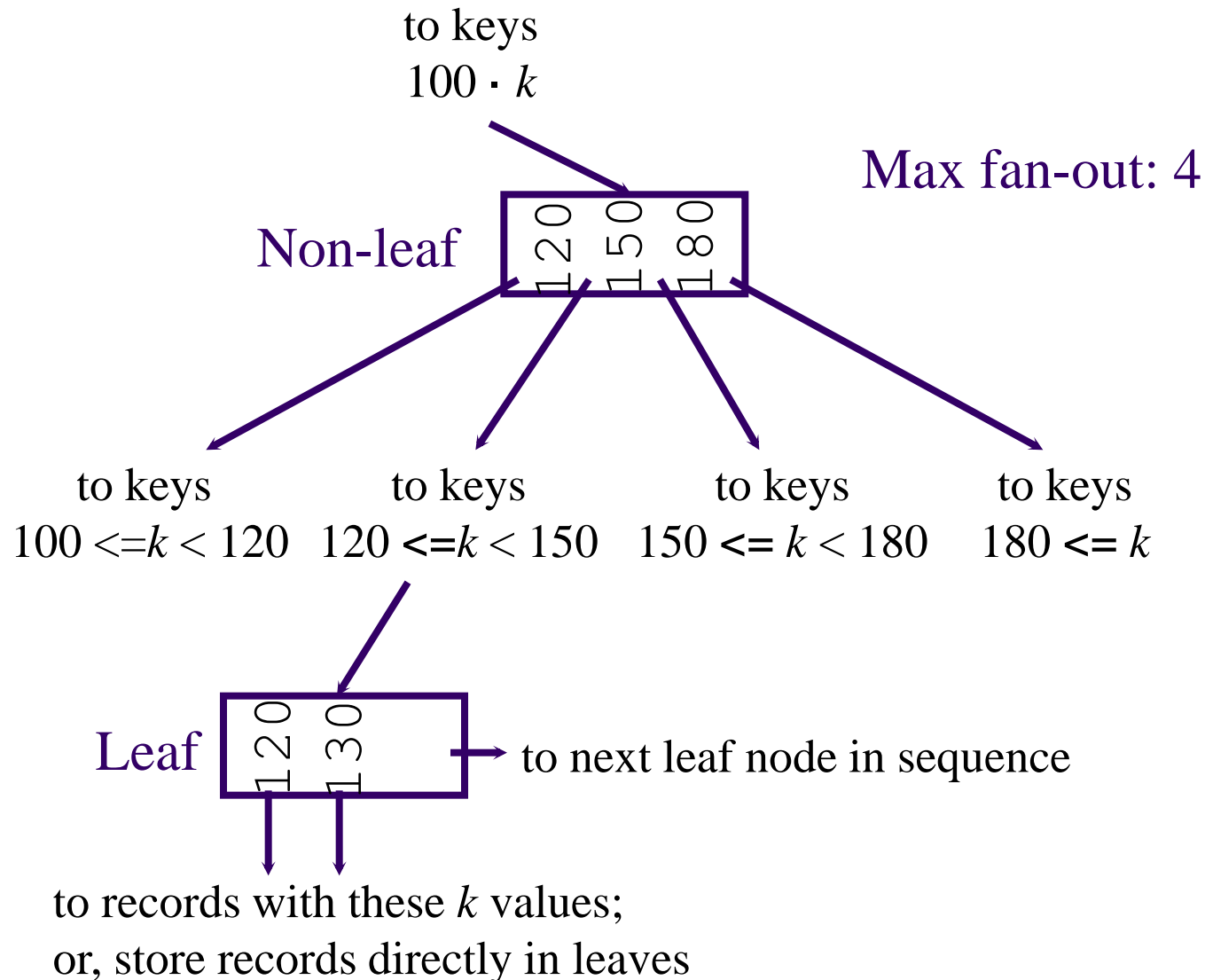
B⁺-tree

- A hierarchy of intervals
- **Balanced** (more or less): good performance guarantee
- **Disk-based**: one node per block; large fan-out

Max fan-out: 4



Sample B⁺-tree nodes



B⁺-tree balancing properties

- Height constraint: all leaves at the same lowest level
- Fan-out constraint: all nodes at least half full (except root)

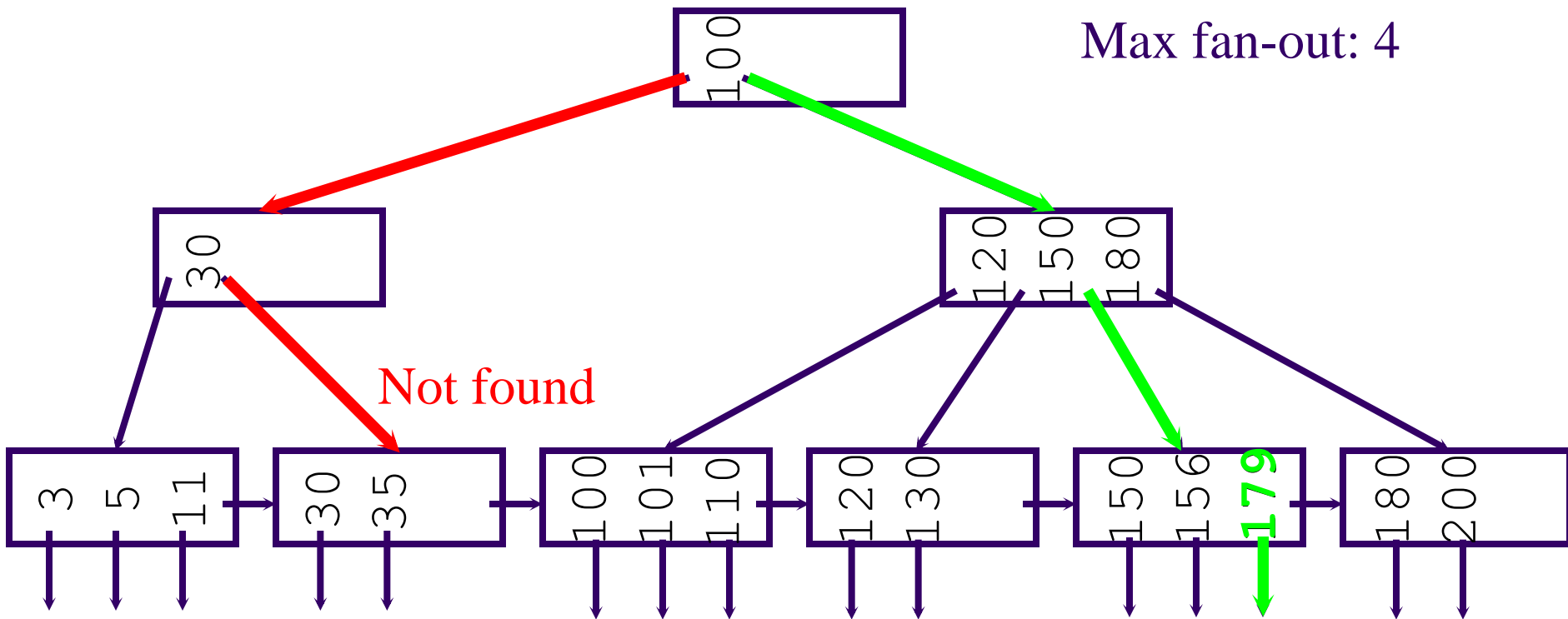
	Max # pointers	Max # keys	Min # active pointers	Min # keys
Non-leaf	f	$f - 1$	$\lceil f / 2 \rceil$	$\lceil f / 2 \rceil - 1$
Root	f	$f - 1$	2	1
Leaf	f	$f - 1$	$\lfloor f / 2 \rfloor$	$\lfloor f / 2 \rfloor$

Lookups

SELECT * FROM *R* WHERE $k = 179$;

SELECT * FROM *R* WHERE $k = 32$;

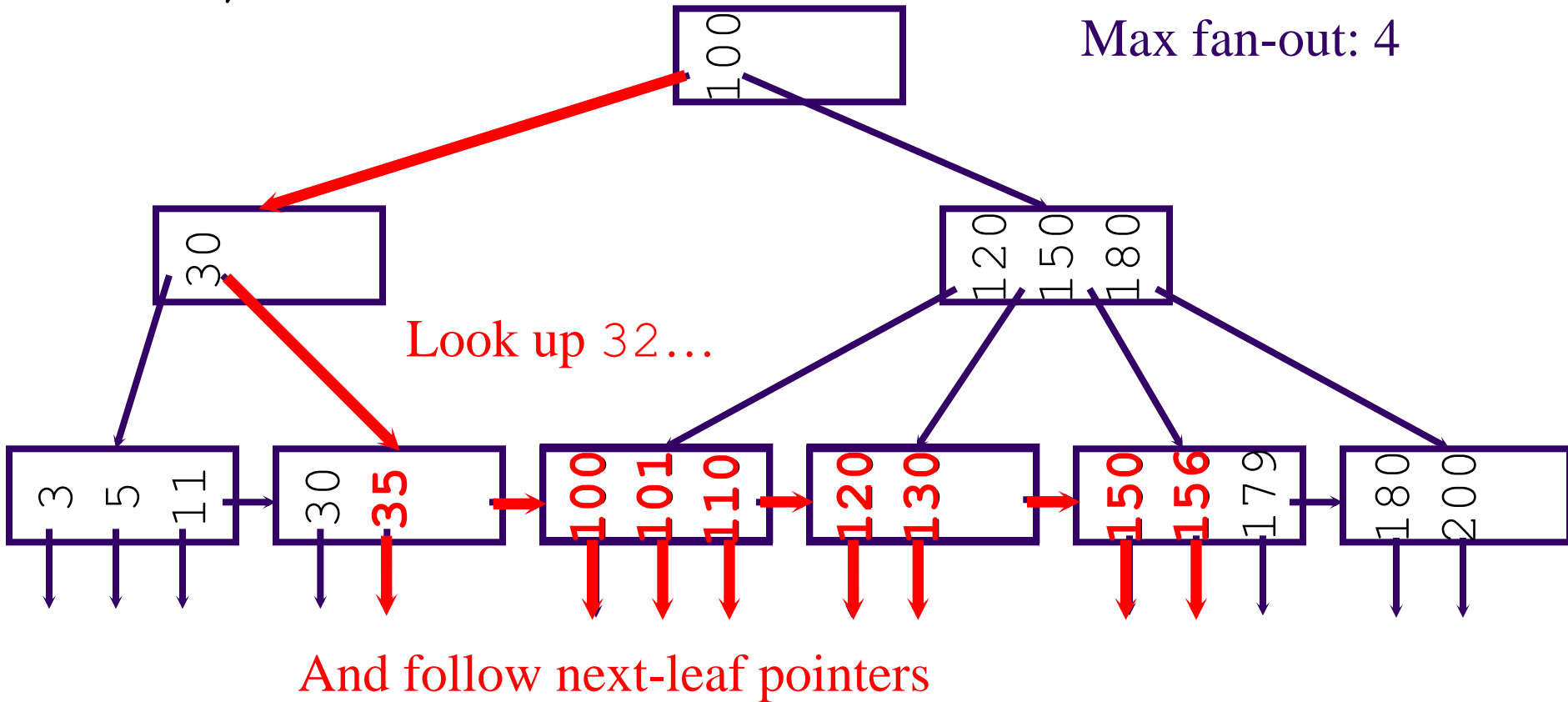
Max fan-out: 4



Range query

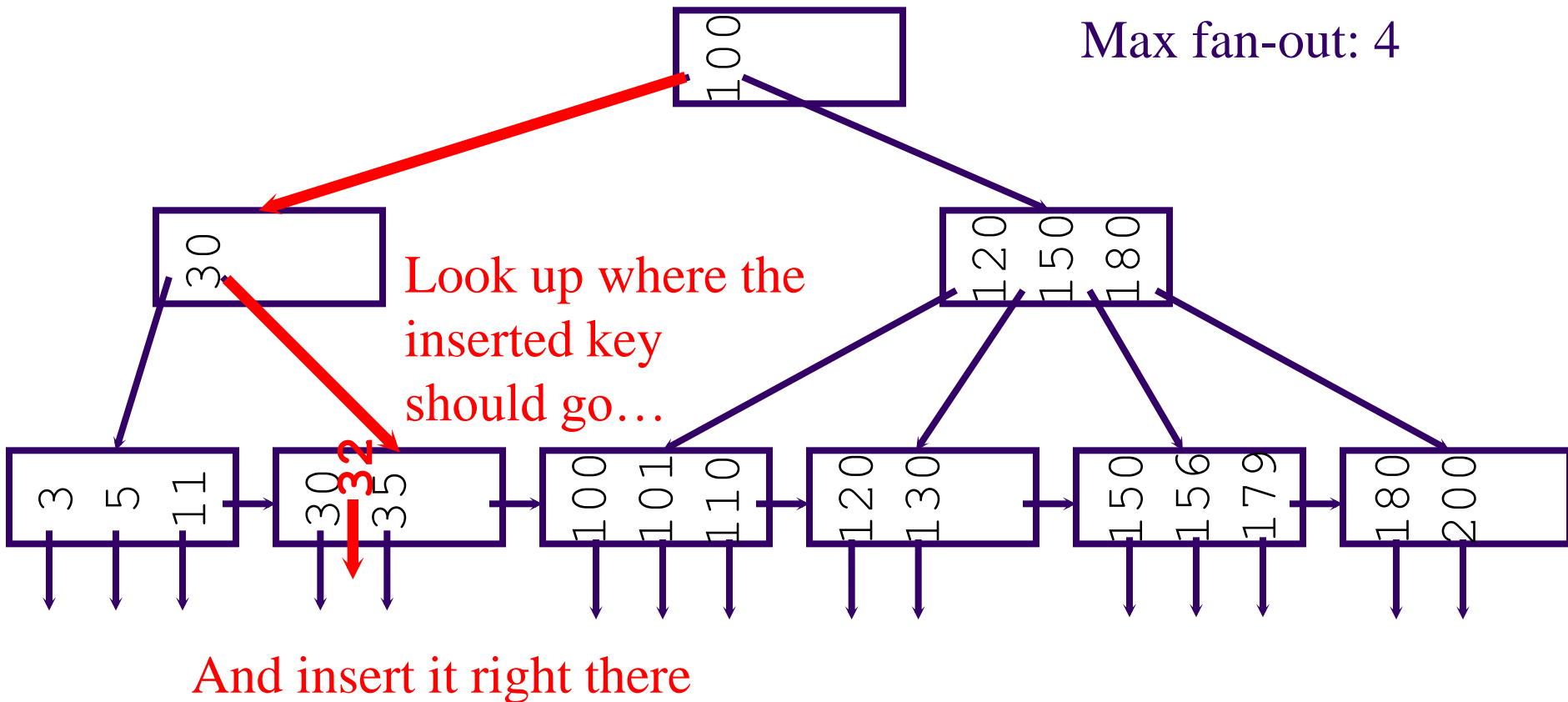
SELECT * FROM *R* WHERE $k > 32$ AND $k < 179$;

Max fan-out: 4



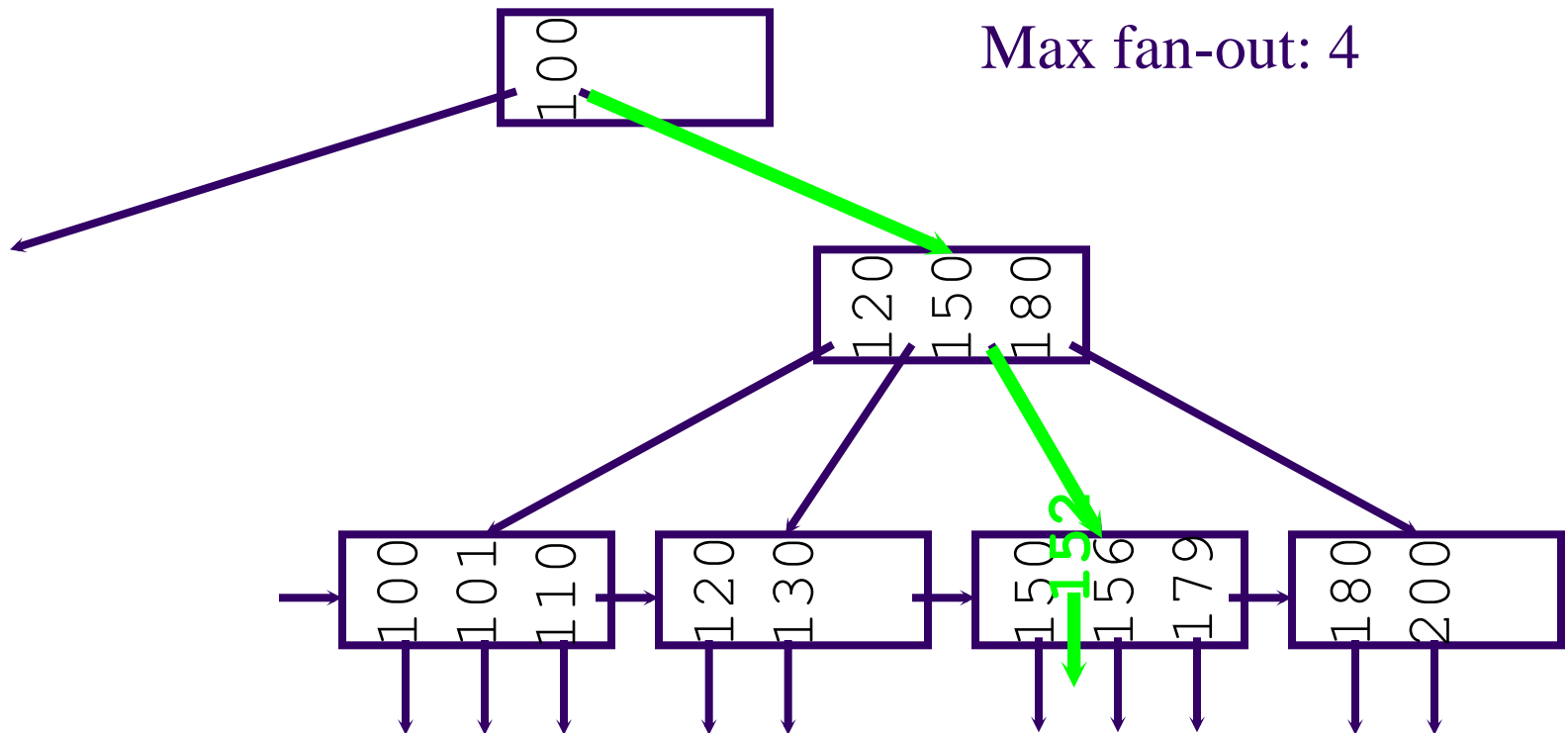
Insertion

- Insert a record with search key value 32



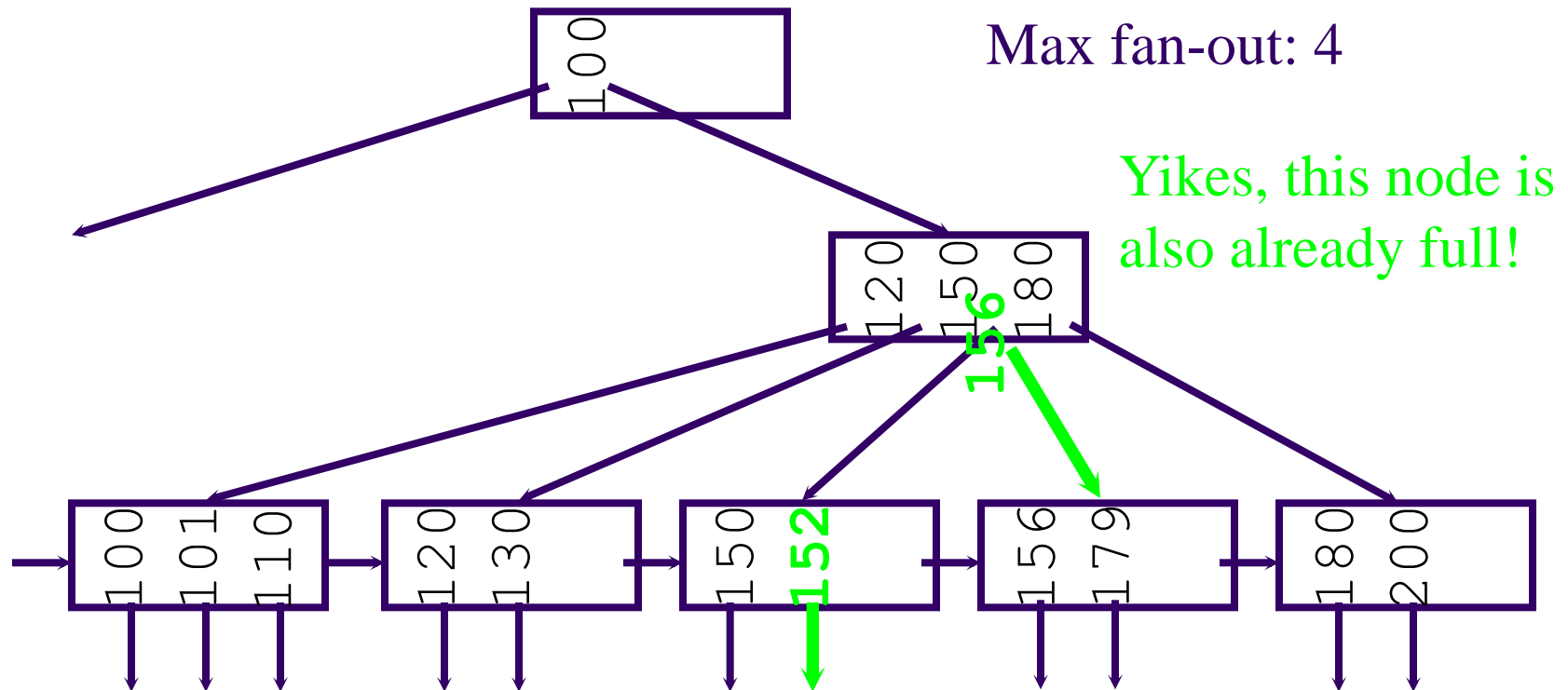
Another insertion example

- Insert a record with search key value 152

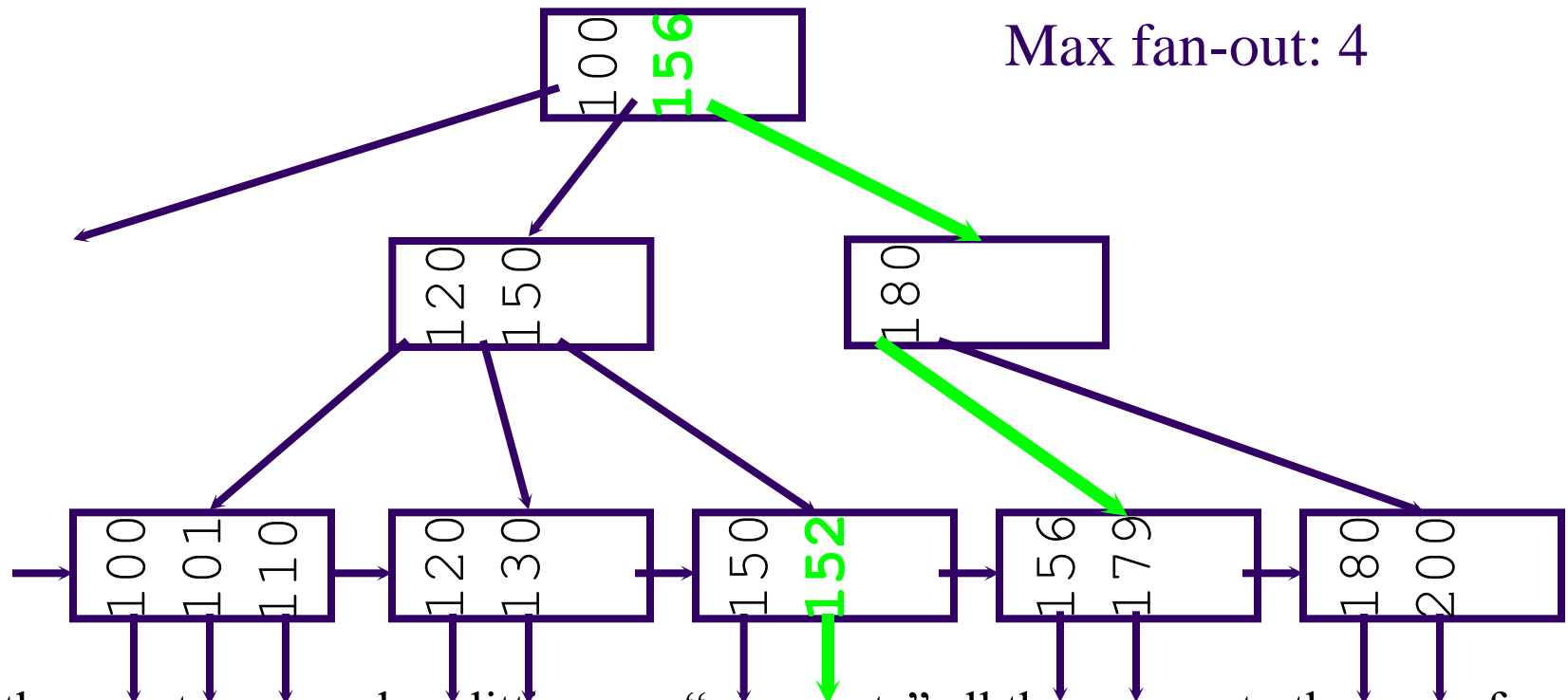


Oops, node is already full!

Node splitting



More node splitting

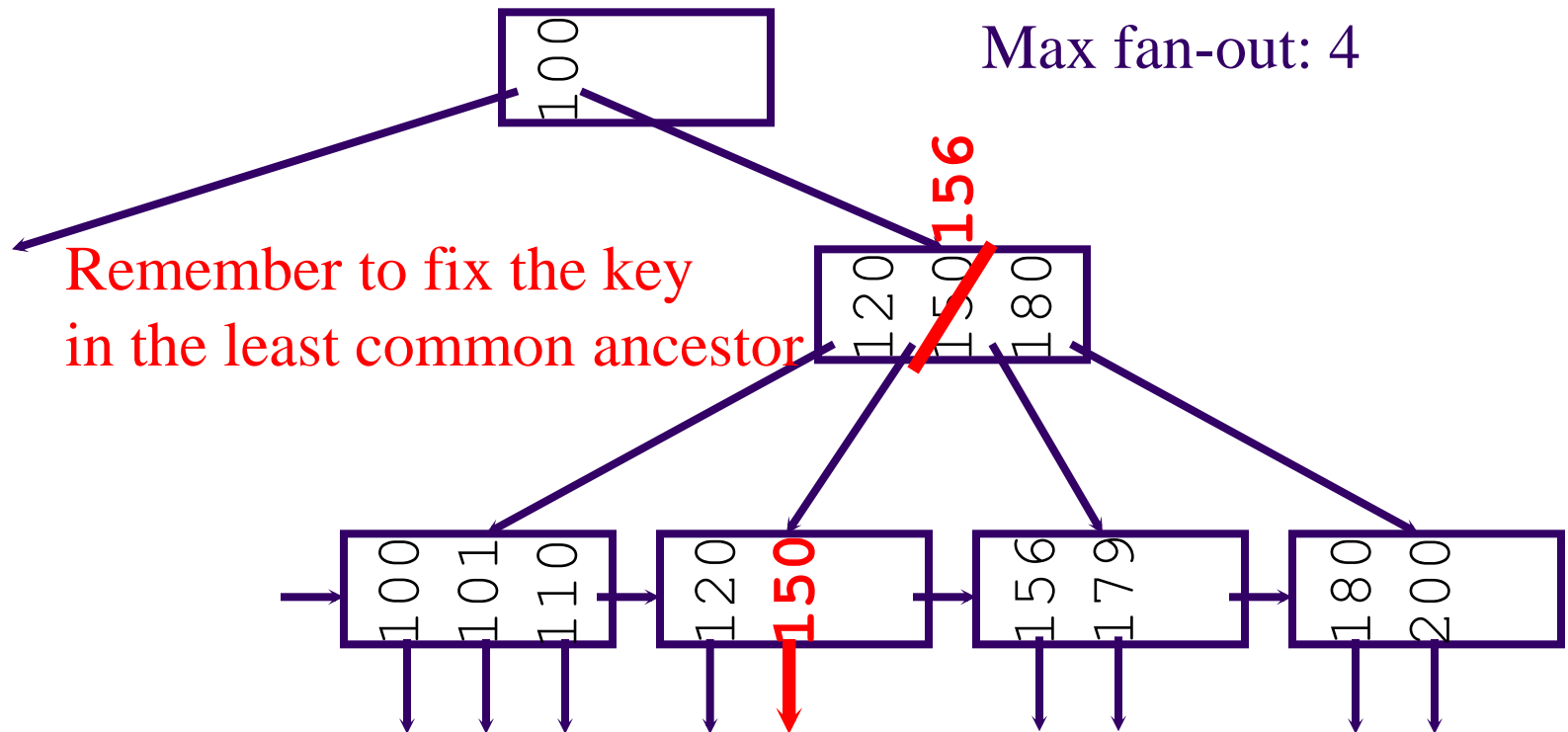


- In the worst case, node splitting can “propagate” all the way up to the root of the tree (not illustrated here)
 - Splitting the root introduces a new root of fan-out 2 and causes the tree to grow “up” by one level

Insertion

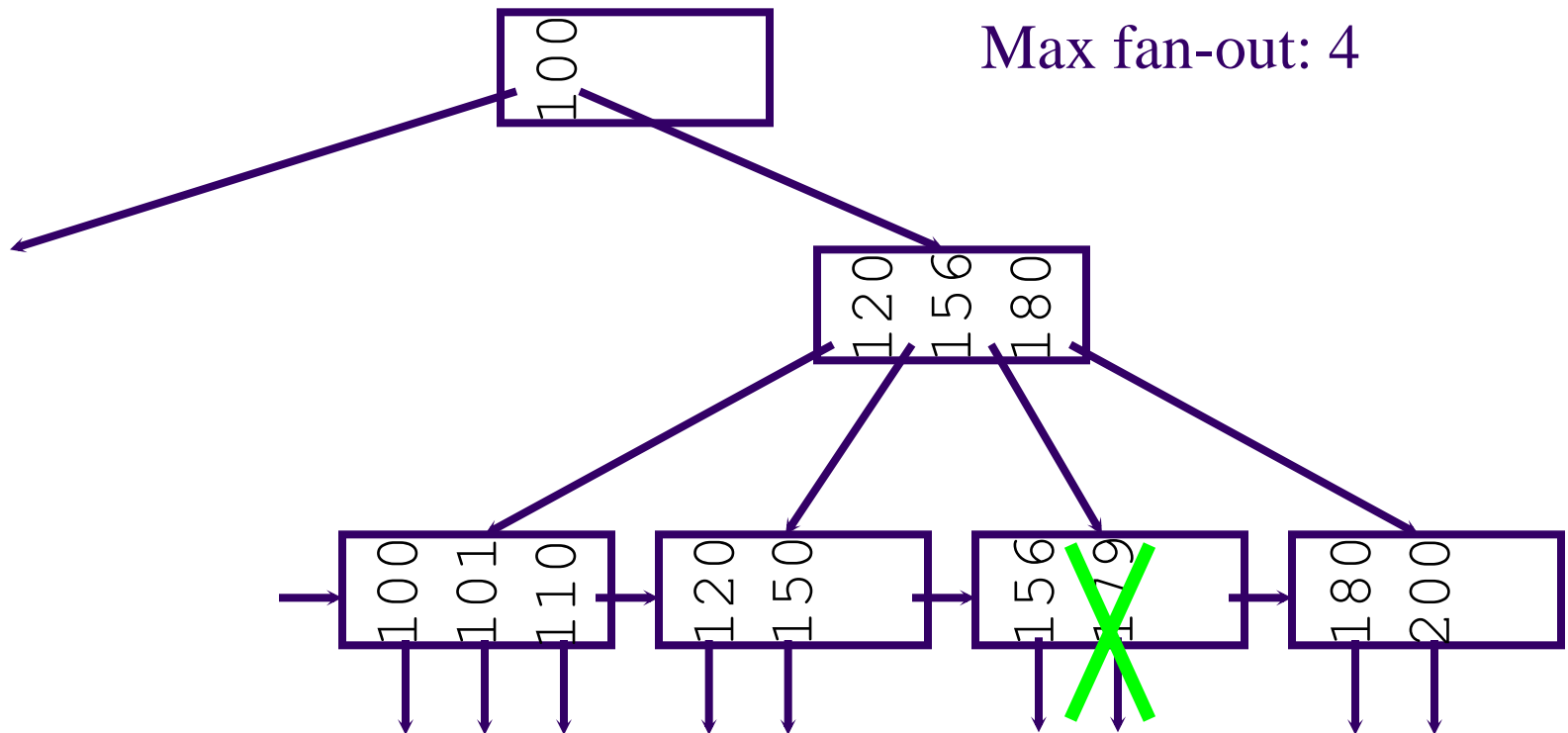
- B⁺-tree Insert
- Find correct leaf L .
- Put data entry onto L .
 - If L has enough space, *done!*
 - Else, must split L (*into L and a new node $L2$*)
 - Distribute entries evenly, copy up middle key.
 - Insert index entry pointing to $L2$ into parent of L .
- This can happen recursively
- Tree growth: gets **wider** and (sometimes) **one level taller at top.**

Stealing from a sibling



Another deletion example

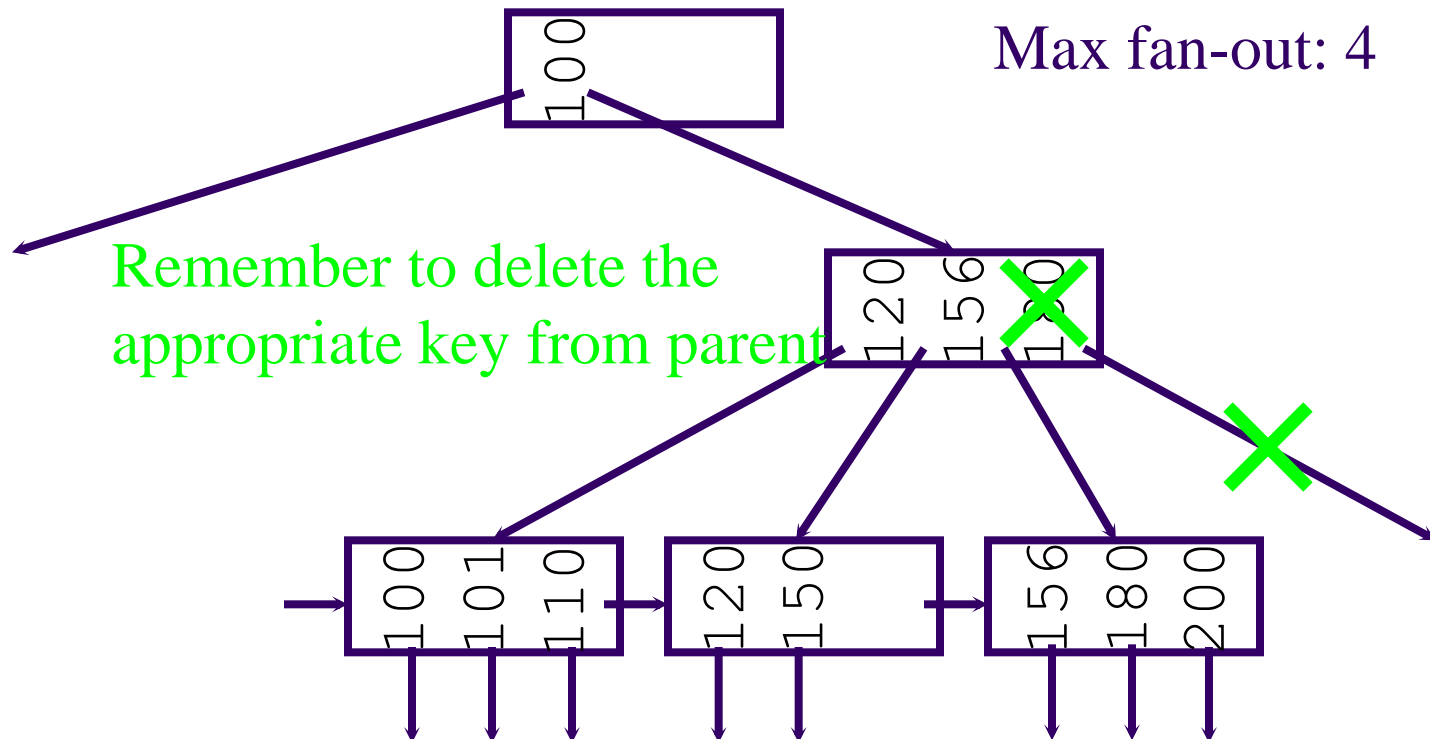
- Delete a record with search key value 179



Cannot steal from siblings

Then coalesce (merge) with a sibling!

Coalescing

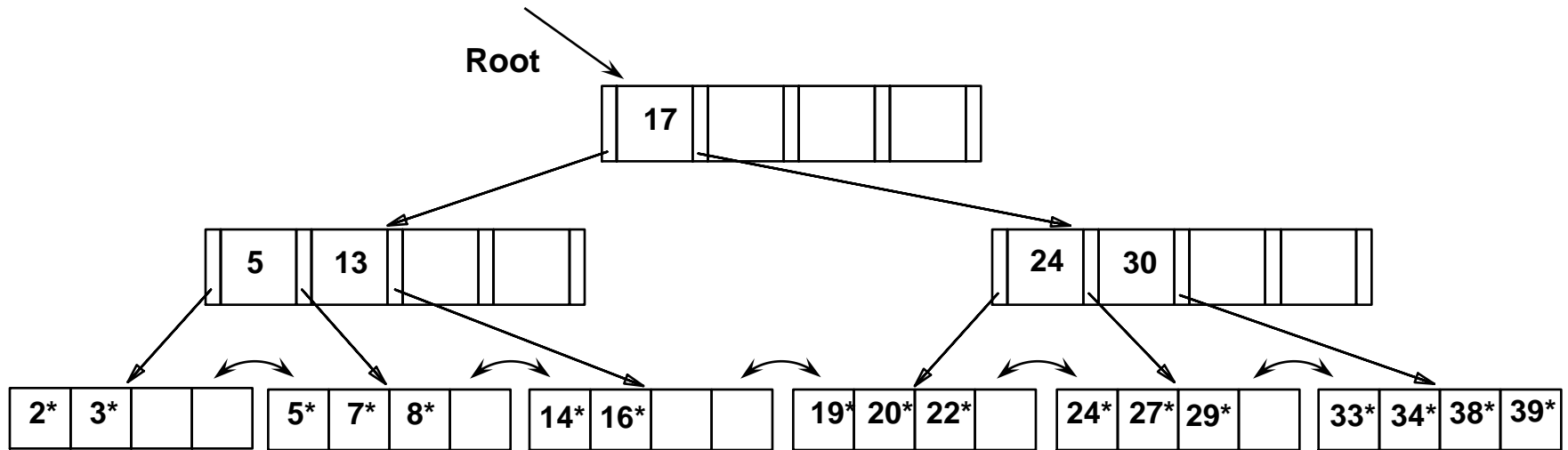


- Deletion can “propagate” all the way up to the root of the tree (not illustrated here)
 - When the root becomes empty, the tree “shrinks” by one level

Deletion

- B+-tree Delete
- Start at root, find leaf L where entry belongs.
- Remove the entry.
 - If L is at least half-full, *done!*
 - If L has only **d-1** entries,
 - Try to redistribute, borrowing from sibling (*adjacent node with same parent as L*).
 - If re-distribution fails, merge L and sibling.
- If merge occurred, must delete entry (pointing to L or sibling) from parent of L .
- Tree shrink: gets **narrower** and (sometimes) **one level lower at top.**

Example B+ Tree - Inserting 8*

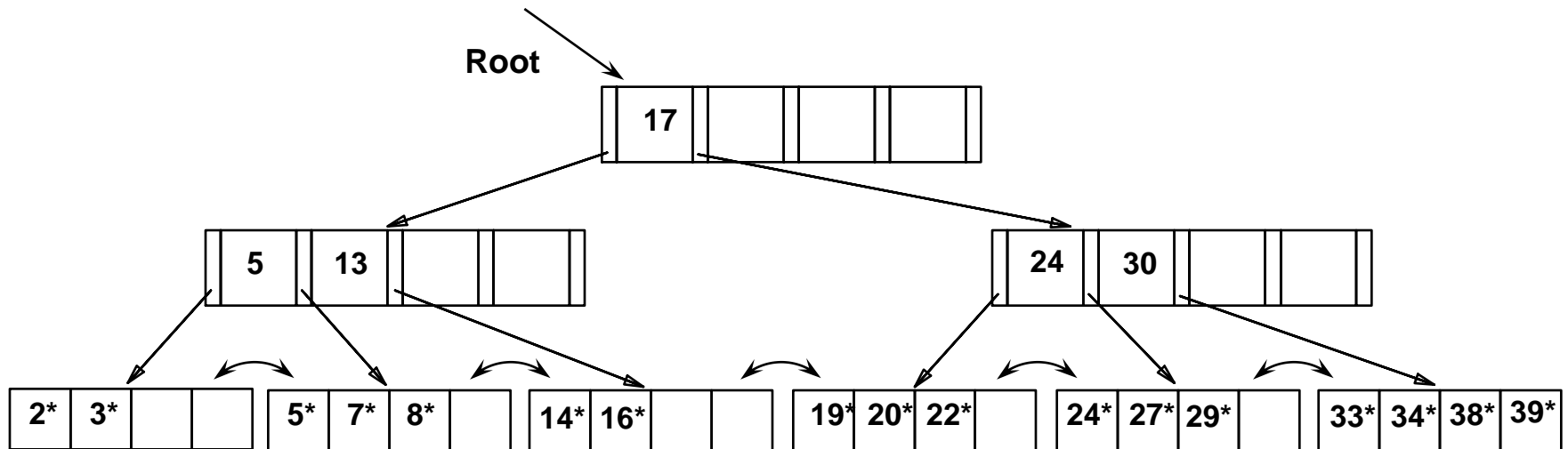


Notice that root was split, leading to increase in height.

In this example, we can avoid split by re-distributing entries; however, this is usually not done in practice.

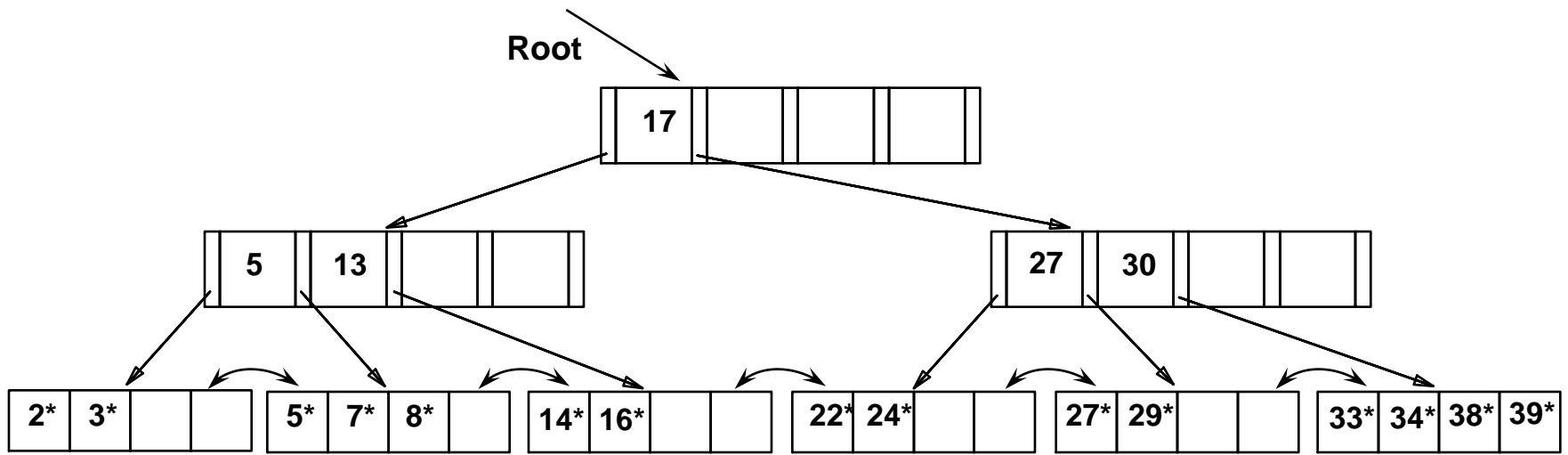
Example Tree (including 8*)

Delete 19* and 20* ...



Example Tree (including 8*)

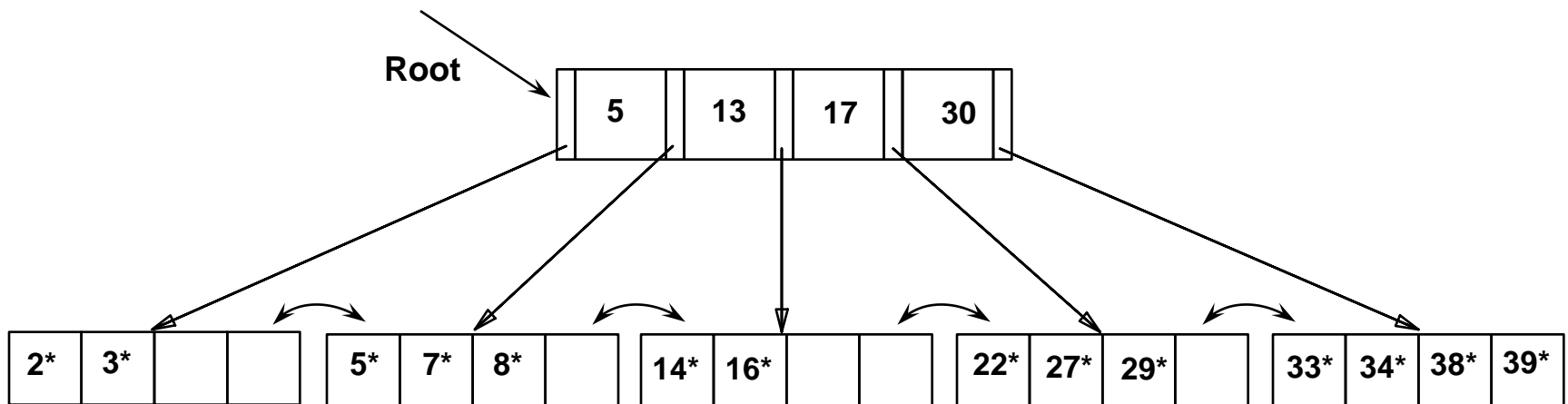
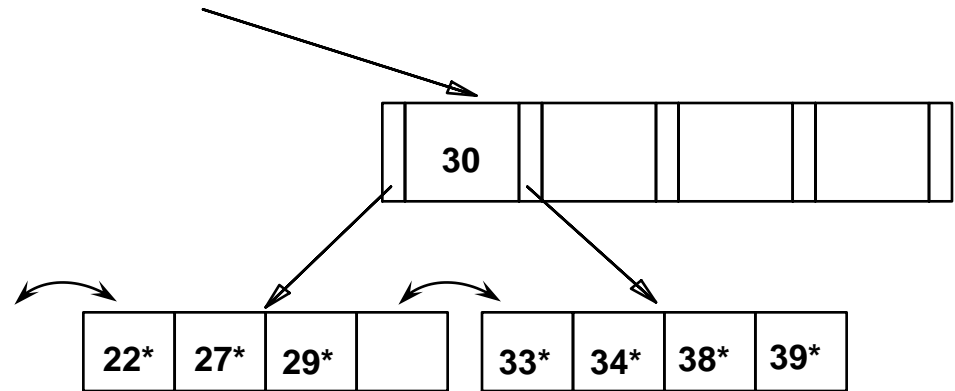
Delete 19* and 20* ...



- Deleting 19* is easy.
- Deleting 20* is done with re-distribution. Notice how middle key is *copied up*.

... And Then Deleting 24*

- Must merge.
- Observe *'toss'* of index entry (key 27 on right), and *'pull down'* of index entry (below).



Performance analysis

- How many I/O's are required for each operation?
 - h , the height of the tree (more or less)
 - Plus one or two to manipulate actual records
 - Plus $O(h)$ for reorganization (should be very rare if f is large)
 - Minus one if we cache the root in memory
- How big is h ?
 - Roughly $\log_{\text{fan-out}} N$, where N is the number of records
 - B⁺-tree properties guarantee that fan-out is least $f/2$ for all non-root nodes
 - Fan-out is typically large (in hundreds)—many keys and pointers can fit into one block
 - A 4-level B⁺-tree is enough for typical tables

B⁺-tree in practice

- Complex reorganization for deletion often is not implemented (e.g., Oracle, Informix)
 - Leave nodes less than half full and periodically reorganize
- Most commercial DBMS use B⁺-tree instead of hashing-based indexes because B⁺-tree handles range queries

The Halloween Problem

- Story from the early days of System R...

```
UPDATE Payroll  
SET salary = salary * 1.1  
WHERE salary >= 100000;
```

- There is a B⁺-tree index on *Payroll(salary)*
- The update never stopped (why?)
- Solutions?
 - Scan index in reverse
 - Before update, scan index to create a complete “to-do” list
 - During update, maintain a “done” list
 - Tag every row with transaction/statement id

B⁺-tree versus ISAM

- ISAM is more **static**; B⁺-tree is more **dynamic**
- ISAM is more compact (at least initially)
 - Fewer levels and I/O's than B⁺-tree
- Overtime, ISAM may not be balanced
 - Cannot provide guaranteed performance as B⁺-tree does

B⁺-tree versus B-tree

- B-tree: why not store records (or record pointers) in non-leaf nodes?
 - These records can be accessed with fewer I/O's
- Problems?
 - Storing more data in a node decreases fan-out and increases h
 - Records in leaves require more I/O's to access
 - Vast majority of the records live in leaves!

Beyond ISAM, B-, and B⁺-trees

- Other tree-based indexes: R-trees and variants, GiST, etc.
- Hashing-based indexes: extensible hashing, linear hashing, etc.
- Text indexes: inverted-list index, suffix arrays, etc.
- Other tricks: bitmap index, bit-sliced index, etc.
 - How about indexing subgraph search?

Summary

- Two types of queries
 - Key-search
 - Range-query
- B⁺-tree operations
 - Search
 - Insert
 - Split child
 - Delete
 - Redistribution
- B⁺-tree sorting
 - Next: disk-based sorting algorithms