

type) compatible; these include UNION, INTERSECTION, and CARTESIAN PRODUCT operation is a set operation that can be applied to two relations, producing all possible combinations. However, we showed how CARTESIAN PRODUCT followed the Cartesian product of sets, and so define matching tuples from two relations and leads to the Cartesian product of the two relations. The Cartesian product of two relations is called THETA JOIN, EQUIJOIN, and is a type of JOIN operation. Query trees were introduced as a graphical representation of queries, which can also be used as the basis for internal representation of queries. Query trees can be used to represent a query.

important types of queries that *cannot* be stated with the basic operations but are important for practical situations. We introduced PROJECTION to use functions of attributes in the projection operation, and AGGREGATE to use functions of aggregate types of attributes. We also introduced SUMMARIZE to summarize the information in the tables. We discussed recursion, which is a way to express queries that cannot be expressed otherwise; there is no direct support in the algebra but which can be expressed using the recursive approach, as we demonstrated. Then we presented the JOIN and UNION operations, which extend JOIN and UNION and preserve the source relations to be preserved in the result.

We described the basic concepts behind relational calculus, which is a type of mathematical logic called predicate calculus. There are two types of relational calculus: (1) the tuple relational calculus, which uses tuples (rows) of relations, and (2) the domain relational calculus, which uses domain variables that range over domains (columns of relations). A query is specified in a single declarative statement, called a query expression, in the tuple relational calculus. In the domain relational calculus, a query is specified in a single declarative statement, called a query expression, in the domain relational calculus. The order or method for retrieving the query result. Hence, relational calculus is considered to be a higher-level *declarative* language than the tuple relational calculus, which is considered to be a lower-level *procedural* language. We use a relational calculus expression states *what* we want to retrieve, and the tuple relational calculus expression states *how* we want to retrieve the query may be executed.

of relational calculus queries using both tuple and domain query graphs as an internal representation for queries in \mathcal{R} . We also discussed the existential quantifier (\exists) and the universal quantifier (\forall) at relational calculus variables are bound by these quantifiers. We then saw how queries with universal quantification are written, and how they can be transformed into existential quantification. The problem of specifying safe queries whose results are finite. We saw how the transformation of universal into existential quantifiers, and vice versa, can be used to transform queries into relational calculus, and that give expressive power to the relational calculus, making it more powerful than the basic relational algebra. There is no analog to grouping and aggregate functions in basic relational calculus, although some extensions have been proposed.

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of relational algebra and the purpose of each.

What is union compatibility? Why do the UNION, INTERSECTION, and DIFFERENCE operations require that the relations on which they are applied be union compatible?

Discuss some types of queries for which renaming of attributes is necessary in order to specify the query unambiguously.

Discuss the various types of *inner join* operations. Why is theta join required?

What role does the concept of *foreign key* play when specifying the most common types of meaningful join operations?

What is the FUNCTION operation? What is it used for?

How are the OUTER JOIN operations different from the INNER JOIN operations? How is the OUTER UNION operation different from UNION?

In what sense does relational calculus differ from relational algebra, and in what sense are they similar?

How does tuple relational calculus differ from domain relational calculus?

1. Discuss the meanings of the existential quantifier (\exists) and the universal quantifier (\forall).

1. Define the following terms with respect to the tuple calculus: *tuple variable*, *range relation*, *atom*, *formula*, and *expression*.

2. Define the following terms with respect to the domain calculus: *domain variable*, *range relation*, *atom*, *formula*, and *expression*.

3. What is meant by a *safe expression* in relational calculus?
4. When is a query language called relationally complete?

Exercises

6.15. Show the result of each of the sample queries in Section 6.5 as it would apply to the database state in Figure 3.6.

11.6. Specify the following queries on the COMPANY relational database schema shown in Figure 5.5, using the relational operators discussed in this chapter. Also show the result of each query as it would apply to the database state in Figure 3.6.

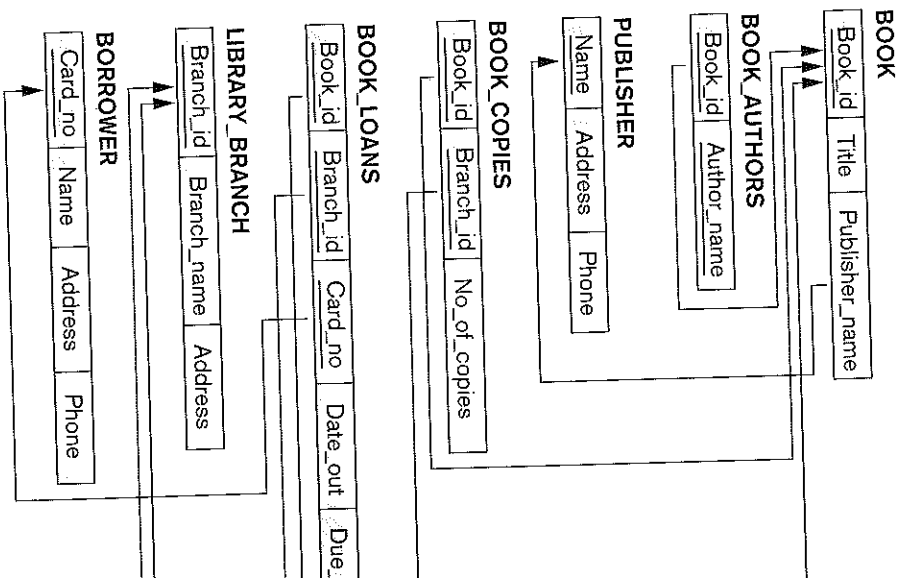
- a. Retrieve the names of all employees in department 5 who work more than 10 hours per week on the ProductX project.

b. List the names of all employees who have a dependent with the same first name as themselves.

c. Find the names of all employees who are directly supervised by 'Franklin Wong'.

d. For each project, list the project name and the total hours per week (by all employees) spent on that project.

- e. Retrieve the names of all employees who work on every project.
 - f. Retrieve the names of all employees who do not work on any project.
 - g. For each department, retrieve the department name and the average salary of all employees working in that department.
 - h. Retrieve the average salary of all female employees.
 - i. Find the names and addresses of all employees who work on at least one project located in Houston but whose department has no location in Houston.
 - j. List the last names of all department managers who have no dependents.
- 6.17. Consider the AIRLINE relational database schema shown in Figure 3.8, which was described in Exercise 3.12. Specify the following queries in relational algebra:
- a. For each flight, list the flight number, the departure airport for the first leg of the flight, and the arrival airport for the last leg of the flight.
 - b. List the flight numbers and weekdays of all flights or flight legs that depart from Houston Intercontinental Airport (airport code 'IAH') and arrive in Los Angeles International Airport (airport code 'LAX').
 - c. List the flight number, departure airport code, scheduled departure time, arrival airport code, scheduled arrival time, and weekdays of all flights or flight legs that depart from some airport in the city of Houston and arrive at some airport in the city of Los Angeles.
 - d. List all fare information for flight number 'CO197'.
 - e. Retrieve the number of available seats for flight number 'CO197' on '2009-10-09'.
- 6.18. Consider the LIBRARY relational database schema shown in Figure 6.14, which is used to keep track of books, borrowers, and book loans. Referential integrity constraints are shown as directed arcs in Figure 6.14, as in the notation of Figure 3.7. Write down relational expressions for the following queries:
- a. How many copies of the book titled *The Lost Tribe* are owned by the library branch whose name is 'Sharpstown'?
 - b. How many copies of the book titled *The Lost Tribe* are owned by each library branch?
 - c. Retrieve the names of all borrowers who do not have any books checked out.
 - d. For each book that is loaned out from the Sharpstown branch and whose Due_date is today, retrieve the book title, the borrower's name, and the borrower's address.
 - e. For each library branch, retrieve the branch name and the total number of books loaned out from that branch.



- 6.19. Specify the following queries in relational algebra on given in Exercise 3.14:
- a. List the Order# and Ship_date for all orders shipped from Jose Lopez was supplied his orders. Produce a listing

Retrieve the names of all employees who work on every project.
Retrieve the names of all employees who do not work on any project.
For each department, retrieve the department name and the average salary of employees working in that department.
Retrieve the average salary of all female employees.
Retrieve the names and addresses of all employees who work on at least one project located in Houston but whose department has no location in Houston.
Retrieve the names of all department managers who have no dependents.
Retrieve the flight number, the departure airport for the first leg of the flight, and the arrival airport for the last leg of the flight.
Retrieve the flight numbers and weekdays of all flights or flight legs that originate from Houston Intercontinental Airport (airport code 'IAH') and terminate at Los Angeles International Airport (airport code 'LAX').
Retrieve the flight number, departure airport code, scheduled departure time, arrival time, scheduled arrival time, and weekdays of all flights or flight legs that depart from some airport in the city of Houston and arrive at an airport in the city of Los Angeles.
Retrieve information for flight number 'CO197'.
Retrieve the number of available seats for flight number 'CO197' on the date '09/01/99'.

Figure 6.14 shows a LIBRARY relational database schema. Referential integrity constraints are shown as directed arcs in Figure 6.14, as in the notation of Figure 3.7. Write down relational expressions for the following queries:
1. Retrieve the names of the book titled *The Lost Tribe* owned by the branch whose name is 'Sharpstown'.
2. Retrieve the names of the book titled *The Lost Tribe* owned by each branch.
3. Retrieve the names of all borrowers who do not have any books checked out from the branch whose name is 'Sharpstown'.
4. Retrieve the book that is loaned out from the Sharpstown branch and whose due date is today, retrieve the book title, the borrower's name, and the borrower's address.
5. For each library branch, retrieve the branch name and the total number of books loaned out from that branch.

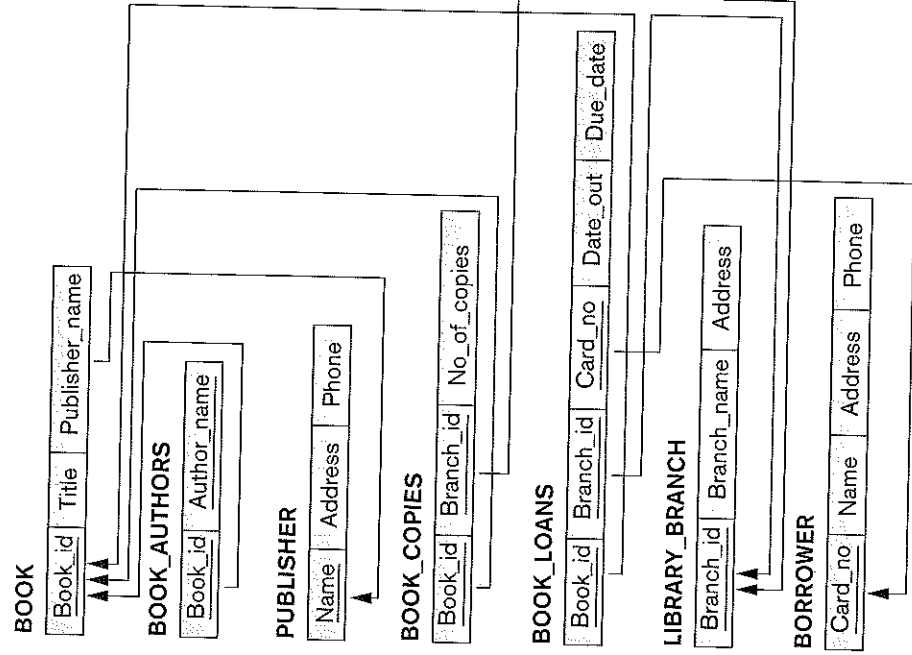


Figure 6.14
A relational database schema for a LIBRARY database.

- f. Retrieve the names, addresses, and number of books checked out for all borrowers who have more than five books checked out.
- g. For each book authored (or coauthored) by Stephen King, retrieve the title and the number of copies owned by the library branch whose name is Central.
- 6.19. Specify the following queries in relational algebra on the database schema given in Exercise 3.14:
- List the Order# and Ship_date for all orders shipped from Warehouse# W2.
 - List the WAREHOUSE information from which the CUSTOMER named Jose Lopez was supplied his orders. Produce a listing: Order#, Warehouse#.

- c. Produce a listing Cname, No_of_orders, Avg_order_amt, where the middle column is the total number of orders by the customer and the last column is the average order amount for that customer.
- d. List the orders that were not shipped within 30 days of ordering.
- e. List the Order# for orders that were shipped from *all* warehouses that the company has in New York.

6.20. Specify the following queries in relational algebra on the database schema given in Exercise 3.15:

- a. Give the details (all attributes of trip relation) for trips that exceeded \$2,000 in expenses.
- b. Print the Ssns of salespeople who took trips to Honolulu.
- c. Print the total trip expenses incurred by the salesperson with SSN = '234-56-7890'.

6.21. Specify the following queries in relational algebra on the database schema given in Exercise 3.16:

- a. List the number of courses taken by all students named John Smith in Winter 2009 (i.e., Quarte='W09').
- b. Produce a list of textbooks (include Course#, Book_isbn, Book_title) for courses offered by the 'CS' department that have used more than two books.
- c. List any department that has all its adopted books published by 'Pearson Publishing'.

6.22. Consider the two tables T1 and T2 shown in Figure 6.15. Show the results of the following operations:

- a. $T1 \bowtie T1.P = T2.A \quad T2$
- b. $T1 \bowtie T1.Q = T2.B \quad T2$
- c. $T1 \bowtie T1.P = T2.A \quad T2$
- d. $T1 \bowtie T1.Q = T2.B \quad T2$
- e. $T1 \cup T2$
- f. $T1 \bowtie (T1.P = T2.A \text{ AND } T1.R = T2.C) \quad T2$

TABLE T1

P	Q	R
10	a	5
15	b	8
25	a	6

TABLE T2

A	B	C
10	b	6
25	c	3
10	b	5

Figure 6.15
A database state for the
relations T1 and T2.

6.23. Specify the following queries in relational algebra on the database schema given in Exercise 3.17:

- a. For the salesperson named 'Jane Doe', list the following all the cars she sold: Serial#, Manufacturer, Sale_price.
- b. List the Serial# and Model of cars that have no options.
- c. Consider the NATURAL JOIN operation between SALE and SALE. What is the meaning of a left outer join for these change the order of relations? Explain with an example.
- d. Write a query in relational algebra involving selection and join and say in words what the query does.

6.24. Specify queries a, b, c, e, f, i, and j of Exercise 6.16 in both tuple relational calculus.

6.25. Specify queries a, b, c, and d of Exercise 6.17 in both tuple relational calculus.

6.26. Specify queries c, d, and f of Exercise 6.18 in both tuple relational calculus.

6.27. In a tuple relational calculus query with n tuple variables, what is the typical minimum number of join conditions? Why? What having a smaller number of join conditions?

6.28. Rewrite the domain relational calculus queries that followed 6.7 in the style of the abbreviated notation of QOA, where the minimize the number of domain variables by writing constraints wherever possible.

6.29. Consider this query: Retrieve the Ssns of employees who work on those projects on which the employee with Ssn=123456789 works. Express this query in tuple relational calculus, using the rules

- x is a tuple variable that ranges over the PROJECT relation.
- $P \equiv \text{EMPLOYEE with Ssn}=123456789 \text{ works on PROJECT } x$.
- $Q \equiv \text{EMPLOYEE } e \text{ works on PROJECT } x$.
- Express the query in tuple relational calculus, using the rules
- $(\forall x)(P(x)) \equiv \text{NOT}(\exists x)(\text{NOT}(P(x)))$.
- $(\text{IF } P \text{ THEN } Q) \equiv (\text{NOT}(P) \text{ OR } Q)$.

6.30. Show how you can specify the following relational algebra queries in both tuple and domain relational calculus.

- a. $\sigma_{A=C}(R(A, B, C))$
- b. $\pi_{\langle A, B \rangle}(R(A, B, C))$
- c. $R(A, B, C) * S(C, D, E)$
- d. $R(A, B, C) \cup S(A, B, C)$
- e. $R(A, B, C) \cap S(A, B, C)$

Relational Calculus

type) compatible; these include UNION, INTERSECTION, and DIFFERENCE. What is union compatibility? Why do the UNION, INTERSECTION, and DIFFERENCE operations require that the relations on which they are applied be compatible? Why is the theta join operation necessary?

1. Discuss some types of queries for which renaming of attributes is necessary. Why is the theta join operation necessary? Why is the theta join operation necessary?

2. Discuss the various types of inner join operations. Why is the theta join operation necessary? Why is the theta join operation necessary?

3. What role does the concept of *foreign key* play when specifying the most common types of meaningful join operations?

4. What is the FUNCTION operation? What is it used for?

5. How are the OUTER JOIN operations different from the INNER JOIN operations? How is the OUTER UNION operation different from UNION?

6. How do relational calculus differ from relational algebra, and in what sense are they similar?

7. How does tuple relational calculus differ from domain relational calculus? Discuss the meanings of the existential quantifier (\exists) and the universal quantifier (\forall).

8. Define the following terms with respect to the tuple calculus: *domain variable*, *range relation*, *atom*, *formula*, and *expression*.

9. Define the following terms with respect to the domain calculus: *domain variable*, *range relation*, *atom*, *formula*, and *expression*.

10. What is meant by a *safe expression* in relational calculus?

11. When is a query language called relationally complete? How does the result of each query as it would apply to the database state in Figure 3.6.

12. How does the result of each query as it would apply to the database state in Figure 3.6.

13. Specify the following queries on the COMPANY relational database schema using relational algebra. Retrieve the names of all employees in department 5 who work more than 10 hours per week on the ProductX project.

- Retrieve the names of all employees in department 5 who work more than 10 hours per week on the ProductX project.
- List the names of all employees who have a dependent with the same first name as themselves.
- Find the names of all employees who are directly supervised by 'Franklin Wong'.
- For each project, list the project name and the total hours per week (by all employees) spent on that project.

Questions

1. Discuss the basic concepts behind relational calculus.

2. Discuss the basic concepts behind relational calculus.

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Exercises

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